

F: Forgotten Fragments

Problem author: Christopher Weyand

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Given a tree and a starting node. You can visit the starting node plus one adjacent subtree. For each possible start, maximize the MEX of the visited nodes.

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- for node 1 the answer is the minimum of all subtrees that do not include node 2

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- other solutions involve segment trees or smaller into larger