G: Garbled Garden

Problem author: Lucas Schwebler, Yidi Zang

Problem

Given an array $t_1, \ldots, t_n$, sort it by applying the minimum number of permutations which have only one cycle of length > 1.

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- Two operations are always sufficient!

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Every permutation is the composition of two cycles.

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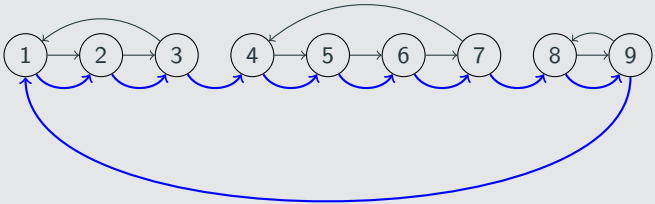

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